

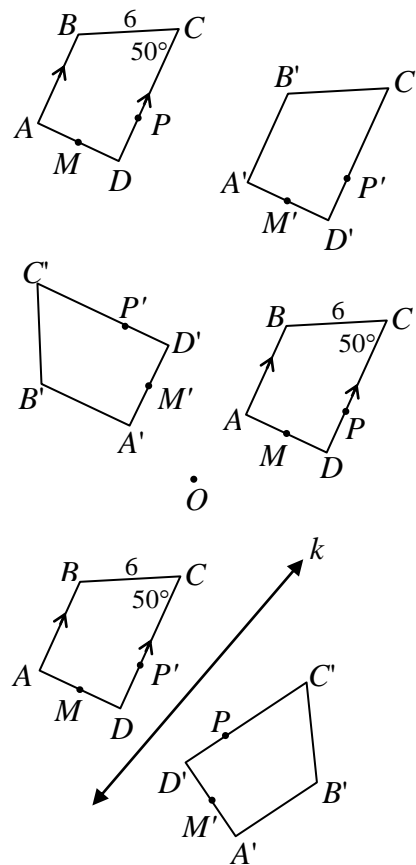
Geometry Notes TG - 8: Rigid Motions

Properties of Certain Transformations

Ex: The diagrams show three transformations of quadrilateral $ABCD$, a translation, a rotation and a reflection. In $ABCD$, we have $BC = 6$, $m\angle C = 50^\circ$, $\overline{DP} \perp \overline{BC}$, $\overline{AB} \parallel \overline{CD}$ and M is the midpoint of \overline{AD} .

Which of the following are true?

	Translation	Rotation	Reflection
$B'C' = 6$	Yes	Yes	Yes
$m\angle C' = 50^\circ$	Yes	Yes	Yes
$\overline{D'P'C'}$	Yes	Yes	Yes
$\overline{A'B'} \parallel \overline{C'D'}$	Yes	Yes	Yes
M' mdpt of $\overline{A'D'}$	Yes	Yes	Yes



We say these transformations "preserve" (keep unchanged) distance, angle measure, collinearity, parallelism and midpoints

If a segment has a certain length, its image will have the same length.

If an angle has a certain measure, its image will have the same measure.

If points are collinear, their images will be collinear.

If two lines are parallel, their images will be parallel.

If M is a midpoint of a certain segment, its image will be the midpoint of the image of the segment.

Rigid Motions

A *rigid motion* is a transformation that

1. preserves distance (length)

The image of a segment will be the same length as the segment

2. preserves angle measure

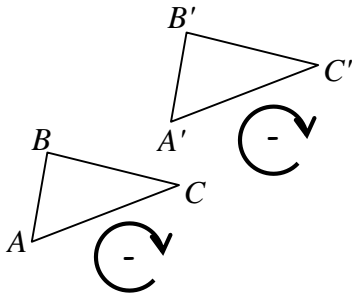
The image of an angle will be the same measure as the angle

Another way of thinking about it: After a rigid motion, the image of any figure will be exactly the same shape and size as the pre-image.

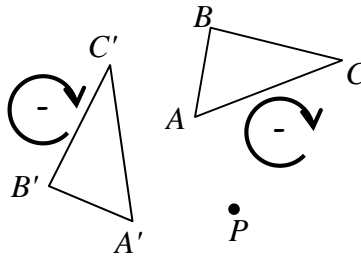
<div style="display: flex; align-items: center;"> <div style="font-size: 2em; margin-right: 5px;">}</div> <div style="margin-right: 10px;"> Translations Rotations Reflections </div> </div>	are all rigid motions.	Also, any composition of translations, rotations and/or reflections will be a rigid motion.
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Orientation

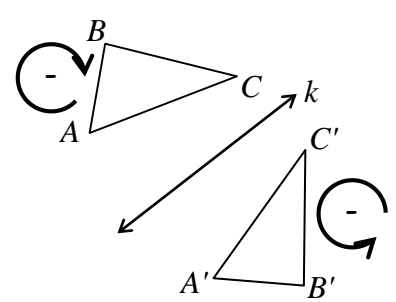
Ex: Translation



Rotation



Reflection



Definition: *Orientation* of a plane figure refers to **order** or **direction** of the vertices.

In all three diagrams above, $\triangle ABC$ is oriented **clockwise**.

Which isometries *preserve orientation*?

Translations and rotations

These are called "direct isometries."

Reflections change orientation: they are "opposite isometries."

A transformation that changes all distances by the same ration is called a **similarity**.

A dilation is a similarity.